

Transmission over Cognitive Radio Channel with Novel Secure LT Code

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ABSTRACT

With the increasing of communication applications in recent years, the demand for radio spectral resources has increased significantly. Cognitive radio scenario was proposed to improve spectrum efficiency in wireless communication systems. In cognitive radio network, it is essential that control information is sent securely and reliably. Ensuring the trustworthiness of the transmitting of spectrum sensing information is important in the CR networks since spectrum sensing directly affects spectrum management and incumbent coexistence. In this paper, the first secondary link channel model is presented, then a secure LT Code is proposed to be compatible with presented channel model and acquires good QoS. As we may know, LT code overcomes packet loss when the channel of the SU is reclaimed by PU. In the new proposed combined encoding and ciphered block, a LT code matrix is used to generate a symmetric cryptographic key. Thus, less complexity observed in the processing computation. Besides, cryptographic key is not sent over the channel. As a result, an attacker has no way to eavesdrop the key unless he is prepared to consider all possible key combinations. This replaced block supplies secure controlling channel and increases spectrum efficiency too.

Keywords: Cognitive Radio; Symmetric Cryptographic Key Generation; LT Code

1. Introduction

With explosive increase in demand for additional frequency spectrum, cognitive radios (CRs) were offered to support existing and new services. CR scenarios were proposed to improve spectrum efficiency and to solve the normally occurring spectrum scarcity. CR is also highly agile wireless platform, so it is capable of autonomously choosing operating parameters based on both frequency spectrum and network conditions. CRs promise an enhanced utilization of the limited spectral resources. In CR scenarios, secondary users (SUs) and primary users (PUs) coexist simultaneously [1-5].

The detection of PUs can be accomplished by opportunistic spectrum sharing [4,6]. In opportunistic spectrum sharing, the PU usage is automatically monitored by SUs based on CR scenario. In the CR scenarios, no changes have to be made to legacy systems as the PU is unaware of the secondary usage of its spectrum. Since the arrival of a PU acts like an erasure on the SU link, it causes the SU to lose all the packets that are being transmitted over the channel which was under that particular PU's carrier. In order to overcome this problem caused by PU arrival

on the SU link, some techniques have been proposed in [7]. In fact, any method to employ some sort of feedback procedures is not practical over CR network, indeed, once the channel has been captured by a PU, the retransmission request has to be placed on a different channel, which may not be available or reliable. So in order to avoid the need for a feedback channel, erasure-correcting codes are suggested [8]. Hence, the packets that are lost due to PU interference are now considered as erasures. The erasure-correcting codes used in our model are digital Fountain codes.

The concept of digital Fountain codes was first introduced by Byers *et al.* [9,10] in 1998 for information distribution. Fountain codes are a class of erasure codes with the property that a potentially limitless sequence of encoding symbols can be generated from a given set of source symbols. The original source symbols can ideally be recovered by the decoder from any subset of the received coded symbols of size equal to or only slightly larger than the number of source symbols. The term fountain or rate less refers to the fact that these codes do not exhibit a fixed code rate. In [11] a solution to further

enhance the performance of cognitive radio networks is proposed.

LT codes were the first practical realization of fountain codes. This code was introduced for the purpose of scalable and fault-tolerant distribution of data over simplex channel like a computer network. Classification of erasure codes is shown in **Table 1**.

LT complexity of the encoding and decoding is very low [8]. Some networks, such as cognitive radio networks, do not have a feedback channel. Applications on these networks still require reliability. The SU link of cognitive radio can be modeled as a two states channel. One state is influenced by channel fading and noise but the other is like erasure channel. Thus, erasure code is a good choice for cognitive radio [12]. On the other hand, in cognitive radio network, it is normal to assume that there are no network attackers and the participants involved in the protocols are honest. But attackers always try to corrupt data anyway. As a result, a secure code is essential that can save time and cost.

As mentioned the successful deployment of CR networks and the realization of their benefits depend on the placement of essential security mechanisms in sufficiently robust form to resist misuse of the systems. Ensuring the trustworthiness of the spectrum sensing process is important in the CR networks, since spectrum sensing directly affects spectrum management and incumbent co-existence [13-17].

In this paper, secondary link channel model is presented and then secure LT code is proposed to supply security and reliability simultaneously. In the proposed block, a code matrix is used for generation of cryptographic key. Cryptographic key is not sent over the channel; as a result, the frequency spectrum is saved. Also coder information is used to generate cryptographic key.

The rest of this paper is organized as follows. In Section 2, we present the channel model of secondary link for cognitive radio. In Section 3, we discuss the proposed block and algorithm to generate symmetric cryptographic key. Simulation results and performance analysis are revealed in Section 4. Section 5 presents concluding remarks.

2. Secondary Link Channel Model for CR

The SU link can be modeled as a two states channel. In

Table 1. Classification of erasure code.

		Conventional	RS
	Fixed Rate		BCH
Erasure Code		LDPC	Tornado
			LT
	Rateless	Fountain	Raptor

the first state, channel is good. A channel is considered good if PU arrives after the duration of SU transmission and packets are lost due to channel fading and noise. In this state, a conventional method can be employed to improve the full system performance. In the other state, the channel is reclaimed by the PU during transmission of SU, then all packets transmitted over that channel after arrival of PU will be lost due to the evacuation of the SU. Hence, in order to recover these packets, some error correcting mechanisms are needed. In this state, the channel model can be assumed as erasure channel. The overall channel state diagram for the secondary link can now be observed by **Figure 1**.

P_{ij} is the transition probability from state i to state j . Depending on the types of PUs, the primary traffic model may be different. In this paper, Primary User Arrival Model was assumed to be of a Poisson distribution.

P_{21} is probability density function (pdf) of at least one PU arrival during transmission of SU and can be given by:

$$P_{21} = 1 - P_{poisson}(x = 0) = 1 - e^{-\lambda} \quad (1)$$

P_{22} is the pdf of that PUs do not request any service and can be given by:

$$P_{22} = 1 - P_{21} = 1 - e^{-\lambda} \quad (2)$$

P_{11} is pdf of time duration that the channel is occupied by PU. P_{11} is exponential and its parameter (λ) depends on the type of the Primary network traffic.

$$P_{11} = P_{exponential}(x < t) = 1 - e^{-\lambda t} \quad (3)$$

P_{12} is pdf of time that the channel is released by PU. This means that the transition probability is calculated from state 1 to state 2 after t second.

$$P_{12} = P_{21} \times P_{11} = (1 - e^{-\lambda})(1 - e^{-\lambda t}) \quad (4)$$

Channel states representations are shown in **Figure 2**. In this Figure p_{e1} , p_{e2} are probability of error in the bad (BEC) and good (BSC) channel states respectively. Effective parameters in p_{e1} include channel fading, noise and interference of PU. But p_{e2} depends only upon channel fading and noise.

LT code is capable of providing protection from the

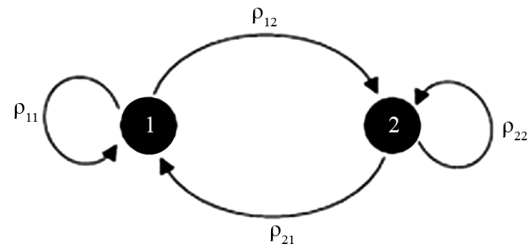


Figure 1. State Diagram of secondary link Channel (1: occupied channel, 2: ideal channel).

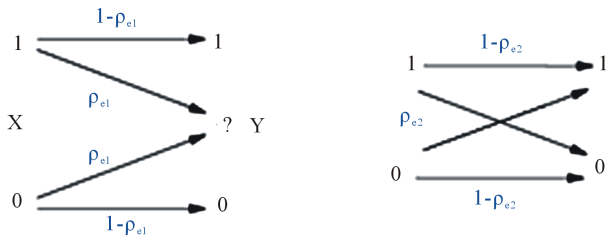


Figure 2. Channel states (a) State 1 (b) state 2. (a) Binary Erasure Channel; (b) Binary Symmetric Channel.

effects of packet loss irrespective of the loss model of the SU link. But the redundancy of the LT code causes to decrease the spectrum efficiency. In fact, in LT codes the reduction in spectrum efficiency is incompatible with the second state of the channel (*i.e.* good state). In order to improve the system's performance a combined block is proposed here. Therefore, a secure LT code (SLC) is designed.

Two types of channels exist in cognitive radio network that are called control and traffic channels. Transmitted information over control channel influences on resource assignment. Thus, to hold good performance transmitted data, control channel should be protected against the attackers and distorting agents.

3. The Proposed Combined Encoding and Cyphering Block

In order to meet security and reliability over networks

such as cognitive radio networks, secure LT code (SLC) is proposed. In this block, coder information is used to generate a sequence of (symmetric) keys k_0, k_1, \dots, k_K . Combination of encryption and channel coder block decreases the required memory and processing time. Process of cryptographic key generation is followed from an algorithm completed by a few random numbers and an input random vector. In other words, a sequence of symmetric key is generated in the transmitter and the receiver and don't need to be sent over the channel. Seed information of random generator is inserted to encrypted input data (X) in two ways. First, they are concatenated to X . In order to increase complexity, the header length can be selected variable periodically. And secondly, they are interleaved by a determined pattern.

The block diagram of a secure LT coder is shown in **Figure 3**. In this block the cryptographic key is generated by the LT code matrix. Thus, overall system has less computation complexity. Besides, cryptographic key is not sent over channel. As a result, attacker has no way to eavesdrop the key, unless he is prepared to consider all possible key combinations. First, the data is encrypted, then the information including seeds of random generator and two random numbers are inserted into encrypted data. Finally Y is coded by LT channel coder to detect and correct error bits. In the receiver, all operations are inverted. In order to insert excess information, one can use a mask or concatenate method. Thus the mask vector must be known for both receiver and transmitter. The

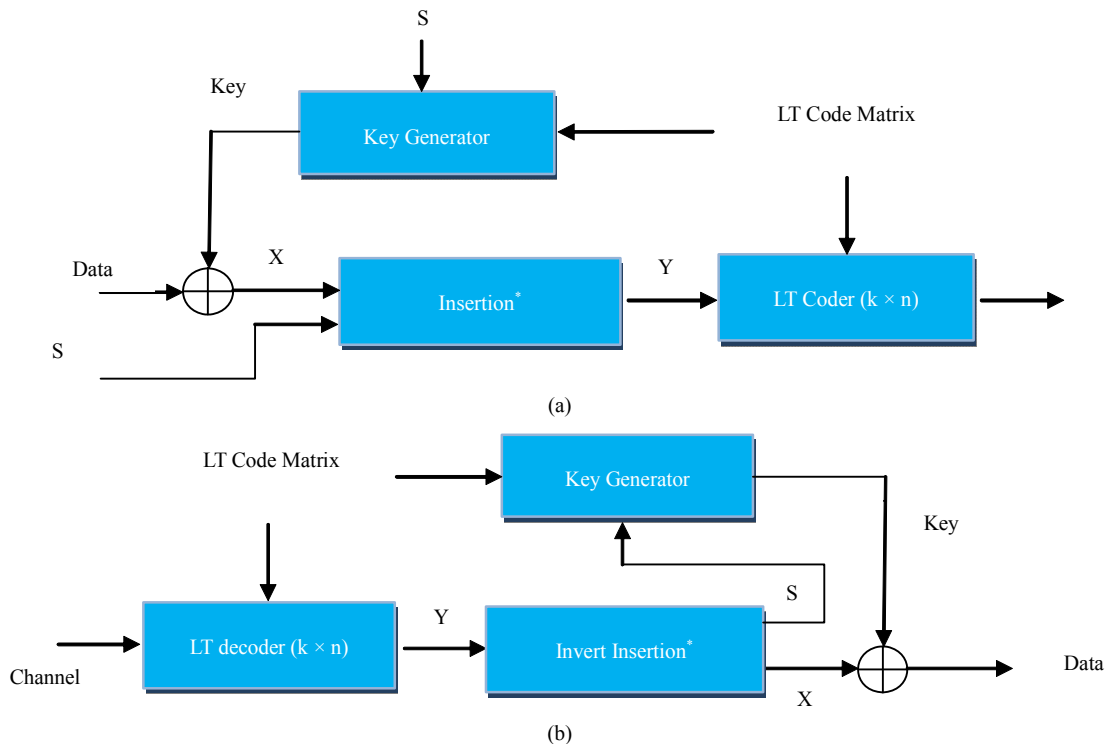


Figure 3. Combined block includes of cryptography and channel coding. (a) Transmitter schematic; (b) Receiver schematic.

block diagram of the transmitter and the receiver are shown in **Figure 3**.

SLC block has two advantages. First one is: a few bits (S packets) are sent instead of a symmetric cryptographic key to supply security of the link. The second advantage that SLC provides is the utilization of LT as error reduction as well as ciphering simultaneously. Indeed, the SLC improves the performance of the system significantly.

Key Generation Process and Management

In the proposed method, key is generated by the code matrix, a random vector and two separate random numbers. Process of key generation is done in both the receiver and the transmitter. In fact, the receiver knows the algorithm as well as receiving their seed values. Therefore, it is not essential to transmit cryptographic key through the channel.

In the designed combined block, the cryptographic symmetric key is generated with LT generator matrix and random numbers. According to the LT codes, its unique and revertible characteristics, the generated sequence of the key includes all possible combinations key. Flow-chart for such a key generation is shown in **Figure 4**. This process can be followed as:

Step 1: A random vector is coded by generator matrix of LT code as.

$$[P]_{1 \times n} = [\text{Input Random Number}]_{1 \times k} \times [G]_{k \times n}$$

where G is the LT code matrix.

Step 2: Hash function is applied to the coded vector.

$$[P_{\text{hash}}]_{1 \times m} = \text{Hash Function}([P]_{1 \times n})$$

where the hash function can be selected arbitrary.

Step 3: The acquired vector is coded by section of generator matrix.

The selection of the section of the generator matrix

The output dimension of the hash function is m bits. In order to encode output of the hash function (m bits), a segment of the LT matrix, with dimensions $m \times k$, has to be selected. Then, two random numbers determine the row and column numbers of the segmented LT matrix.

k_1, n_1 are two random numbers determined from the beginning of the row and the columns of LT matrix (G)

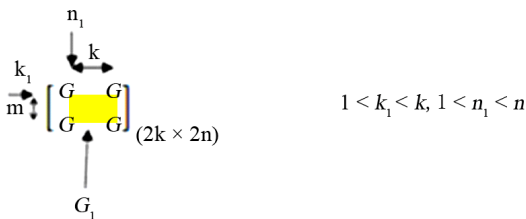


Figure 4. Generation algorithm of matrix G_1 .

to select G_1 . When $(k_1 + m)$ and $(n_1 + k)$ exceed from k and n correspondingly, G is repeated twice in both dimensions to generate G_1 . G_1 generation algorithm is depicted structurally and visually in **Figure 4**.

- Encoding the output of hash function by G_1 to get the actual key:

$$[\text{Key}]_{1 \times k} = [P_{\text{hash}}]_{1 \times m} \times [G_1]_{m \times k}$$

Note: the selection of a section is done by substitution and permutation of the LT generator matrix. Information of this substitution, permutation, seed of random vector and the two random numbers will be transmitted in S packet.

G1 generation algorithm
If $k_1 + m < k, n_1 + k < n$ $G_1 = G[k_1: k_1 + m - 1, n_1: n_1 + k - 1]$
If else $k_1 + m < k, n_1 + k > n$ $n_c = [n_1: n_1 + k - n + n_1]$ $G_1 = G[k_1: k_1 + m - 1, n_c]$
If else $k_1 + m > k, n_1 + k < n$ $n_r = [k_1: k_1 + m - k + k_1]$ $G_1 = G[n_r, n_1: n_1 + k - 1]$
else $n_r = [k_1: k_1 + m - k + k_1]$ $n_c = [n_1: n_1 + k - n + n_1]$ $G_1 = G[n_r, n_c]$

4. Simulation Results

Performance of the key generator is considered via simulation process shown in **Figure 5**. Considering the structure of LT code matrix, we know that the coder has a unique output. Thus, the sequence of key achieved can be swept through all space of 2^k . In order to consider performance of proposed key generation algorithm, simulation was done with the set of parameters followed.

4.1. Parameterization

- 1) LT codes: for LT codes, the degree distribution Ω (d)

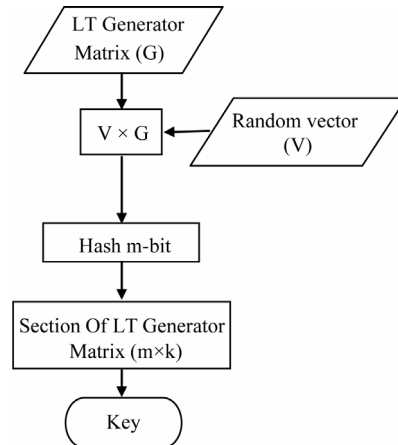


Figure 5. Flowchart of the key generator.

that we use is the robust Soliton distribution and is defined as follows. It has two parameters, σ and δ . The parameter δ is a bound on the probability that the decoding fails to run to completion. The parameter σ adjusts the size of ripple (S). In the paper, we take $\sigma = 0.1$, $\delta = 0.5$, $K = 1000$, $N = 2000$. Now, define:

$$S = \sigma \ln\left(\frac{K}{\delta}\right) \sqrt{K} \quad (5)$$

Then defined,

$$\tau(d) = \begin{cases} \left(\frac{S}{K}\right) \frac{1}{d}, & \text{for } d = 1, 2, \dots, L, \left(\frac{K}{S}\right) - 1 \\ \left(\frac{S}{K}\right) \ln\left(\frac{S}{\delta}\right), & \text{for } d = \left(\frac{K}{S}\right) \\ 0, & \text{for } d = \left(\frac{K}{S}\right) + 1, L, \dots, K \end{cases} \quad (6)$$

$$\rho(d) = \begin{cases} \frac{1}{K}, & \text{for } d = 1 \\ \frac{1}{d(d-1)}, & \text{for } d = 2, 3, \dots, K \end{cases} \quad (7)$$

Then, the Robust Soliton Distribution is obtained by a linear combination of the Ideal Soliton Distribution and $\tau(d)$:

$$\Omega(d) = \frac{\rho(d) + \tau(d)}{\beta}, N = \beta \times K \quad (8)$$

where β is normalization constant. Further discussion and reasoning for this distribution can be found in the references.

2) Random vector with uniform distribution as mask.

3) Hash function: SHA1 is used in simulation. But any hash function can be used.

4) Coding hash function output with section of LT generator matrix ($m \times k$). Generation of two integer random number that indicated number of row and column.

$r = \text{randint}(1, 1, [1, m])$

$c = \text{randint}(1, 1, [1, k])$

5) Insertion pattern: simulation is carried out without pattern and seed information of random generator is concatenated to encrypted input data (X).

4.2. Performance Analysis

This method is resistant against all type of attacks except Brute-Force. Of course, the complexity of the Brute Force attack is highly relative to the available time of the attacker. The number of operators increases exponentially by k input packets. n , k , m are numbers of coded packets, number of input packet, and length of hash functions output respectively. The number of key combinations for Brute-Force attack is computed from Equa-

tion (9).

$$\text{No. state} = 2^n \binom{n}{k} \binom{k}{m} > 2^k \quad (9)$$

According to the number key states and LT code properties, unique and reversible, it can be concluded that the cryptography key is pseudorandom.

5. Conclusion

The importance of security in a cognitive radio network must highly be recognized. Since CR scenario permits attackers to easy and unauthorized access. First of all, secondary link channel model is proposed and a combinational block is proposed for a secure LT code, as well as providing security and error correction capability simultaneously. In SLC, a generator matrix is used to generate a random cryptographic key. SLC supply security without transmitting the key in a symmetric cryptography in a secure channel, as a result, the increase in spectrum efficiency becomes apparent. This implies saving time and costs. Besides, the key does not appear on channel, consequently, the attackers have to consider all possible key combinations. This block is useful in all communication systems that have no feedback channel.

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