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# **Containing SARS COV 2 (COVID 19) through Social Distancing**

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*Author's contribution*

*The sole author designed, analysed, interpreted and prepared the manuscript.*

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# **Abstract**

2019-nCoV/SARS-CoV2 is a highly pathogenic human corona virus transmitted by respiratory droplets with an incubation period of 2-14 days. It is both a public health and economic threat worldwide. In this study, a deterministic mathematical model based on systems of ordinary differential equations for the dynamics of 2019-nCoV/SARS-CoV2 transmission incorporating social distancing as a control measure has been derived. The steady states have also been analysed for stability using the basic reproduction number. Numerical simulations carried out using MATLAB R2021b shows that social distancing intervention is key to reduction in the infection rate of 2019-nCoV/SARS-nCoV2. This study recommends implementation of public policies on public gatherings such as political rallies, worship centers,market places, football matches to curb the potential chain transmission in a pandemic contagion.

*Keywords: Basic reproduction number; Lyapunov functions; global stability; mathematical modeling.*

**2010 Mathematics Subject Classification:** 34C60, 34D23, 37B25, 92B05, 97M60.

# **1 Introduction**

Coronavirus belongs to *Nidovirales* order which include Coronaviridae, Arteriviridae and Roniviridae. Nidovirales order are enveloped, non-segmented positive-sense RNA viruses. Coronaviridae has the

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largest identified RNA genome, [1]. Severely Acute Respiratory Syndrome (SARS)first appeared in Guangdong, China, in November 2002, [2, 3]. This epidemic spread rapidly in the winter of 2003-2004 to many parts of the world, making it the first major disease outbreak of the 21*st* century.

SARS associated Coronavirus (SARS-CoV) was identified as the etiological (causal) agent of SARS, [4]. Prior to SARS-CoV outbre[ak](#page-17-0), Coronaviruses were only thought to cause mild self limiting respiratory infections in human [5]. These vir[us](#page-17-1)[es](#page-17-2) were assumed to be endemic in human populations and was evidently more severe in neonates, elderly and individuals with underlying health conditions. Moreover SARS-CoV transmission was relatively inefficient since it could only be spread through contact with infected individual after the onset of illness. The outbreak was largely contained within [ho](#page-17-3)useholds and health care sett[in](#page-17-4)gs, [6]. An individual could only super-spread the virus through multiple contacts due to enhanced developments of high viral burden, ability to aerosolize the virus or due to compromised immune system [7, 1].

Later in the decade a highly pathogenic human Coronavirus (HCoV) called Middle East Respiratory Syndrome (MERS-CoV) emerging fro[m](#page-17-5) animal reservoir with high mortality was also identified, [8]. Most recently, another highly pathogenic human coronavirus (HCoVs) named 2019 novel Coronavirus (2019-nCoV/SARS-CoV2)has been iden[tifi](#page-17-6)[ed](#page-17-0) as the etiological agent of coronavirus disease 2019 abbreviated as COVID 19. This disease was first reported in Wuhan city, China, in December, 2019, [9]. Viruses such as the human coronavirus (HCoV) require host cellular factors for successful replication during infection [10], hence systematic identification of virus-host protein-protein inter[ac](#page-17-7)tion offer an effective way of eliminating viral infection including SARS-CoV, MERS-CoV and 2019 nCoV. Signs and symptoms of patients with 2019-nCoV infection includes fever, cough and shortness of breath. Based on the incubation of MERS-CoV and SARS which are transmitted by respiratory drople[ts](#page-17-8). Anita and Jerigan, [7] reiterates that COVID 19 occurs within 2-14 days. 2019-nCoV has impacted countries worldwi[de](#page-17-9) causing severe illness and its human to human transmission makes it a public heath and economic threat. Even with the few vaccines like Mordana mRNA-1273, Pfizer-BioNTech BNT162b2, Oxford-AstraZeneca AZD1222-SII Covishield(chAdox1-S), Novavax - NVX CoV2373 that require boost shots after short intervals for their effectiveness and may have some side effects, stringent p[ub](#page-17-6)lic health surveillance systems like identification of cases from high risk countries coupled with rapid diagnostic testing, social distancing and quarantine during an outbreak, [1] should be implemented to curb the potential chain transmission of human coronavirus like this deadly 2019-nCoV/SARS-CoV2.

Transmission of infectious diseases is of great interest to both medics and scholars, [11]. Public heath programm[es](#page-17-0) such as isolation,quarantine,social distancing awareness are strategic in prevention, control and containing an epidemic can subsequently impact the rate of disease transmission in an epidemic contagion, [12].

Mathematical models of COVID 19 have attempted to study both the epidemiologi[cal](#page-17-10) and dynamical aspects of the disease, [7, 13, 14, 15, 16, 17, 18, 19, 8]. From epidemiological perspective, the mathematical models have been used to determine the basic reproduction number [15, 19]. Other models have been t[o e](#page-17-11)stimate the effectiveness of information during the outbreak [15]. The specific dynamics of the disease has also been done by [14]. This study proposes formulation of a mathematical model [o](#page-17-6)f [20](#page-17-12)[19-n](#page-17-13)[CoV](#page-17-14)[/SA](#page-18-0)[RS](#page-18-1)-[Co](#page-18-2)[V2 w](#page-18-3)[it](#page-17-7)h Social Distancing as a Control Measure.

# **2 Objective**

In this paper, we

- 1. Formulate a Mathematical model for 2019-nCoV transmission incorporating social distancing as a control measure.
- 2. Perform stability analysis of the formulated model



**Fig. 1. The flow chart showing dynamics of 2019-nCoV Transmission and Control**

## **3 Model**

This study proposes a deterministic model based on system of ordinary differential equations for the dynamics of 2019-nCoV transmission, incorporating social distancing as a control strategy. The total population at any time *t*,  $N(t)$  is subdivided into 4 compartments: Susceptible  $S(t)$  in which all individuals are susceptible to 2019-nCoV, Social distancing compartment *D*(*t*) , in which individuals are aware about through social distancing as a control and other prevention measures.  $I(t)$  is the compartment in which individuals are infected by 2019-nCoV and Recovered compartment *R*(*t*) in which all individuals have recovered after treatment. Because of the short incubation and assuming that the probability of survival till infectious state for exposed individuals to 2019-nCoV is unity and therefore excluding the exposure stage. The removed class comprises of those who have been removed from scene of infection by means of infection-acquired immunity and death.

The human population is not assumed to be constant since birth, migration, immigration and death occur. The recruitment into *S* susceptible population takes place at the rate  $\Lambda N = \pi$ ,. Natural death rate occurs in *S, D, I* and *R* classes at a rate *µ* . Infected individuals again suffer death due to disease at the rate *σ*. The rate at which susceptible observe social distance is represented by *ξ* where  $0 < \xi < 1$ . Individuals in a susceptible class may acquire infection from infected environment or from infected humans and move to compartment *I* at the rate *βSI* where *β* is the effective contact rate for the disease transmission. Observation of social distance may not be very effective due to search of basic human needs like food so the individuals in class *D* may be infected at the rate  $(1 - \delta)\beta DI$  where  $\delta$  is the success rate of observation of social distancing and  $(1 - \delta)$  is the failure rate of observation of social distancing. Individuals in *I* recover at the rate *κ*.





From the above descriptions of variables and parameters of the flow chart in Fig. 1 we have the following model with non-negative initial conditions

<span id="page-3-0"></span>
$$
\begin{aligned}\n\frac{dS}{dt} &= \pi - \beta SI - \mu S - \xi S \\
\frac{dD}{dt} &= \xi S - \mu D - (1 - \delta)\beta DI \\
\frac{dI}{dt} &= \beta SI + (1 - \delta)\beta DI - (\sigma + \mu + \kappa)I \\
\frac{dR}{dt} &= \kappa I - \mu R\n\end{aligned} \tag{3.1}
$$

### **3.1 Positivity of solutions**

Assuming the initial condition of the system (3.1) to be non-negative

$$
S(0) = S_0 \ge 0, \quad D(0) = D_0 \ge 0, \quad I(0) = I_0 \ge 0, \quad R(0) = R_0 \ge 0
$$

Consider the first equation of the model system (3.1) at time *t*

$$
\frac{dS}{dt} = \pi - \beta SI - \mu S - ES
$$

implying that

$$
\frac{dS}{dt} \ge -\beta SI - \mu S - \xi S
$$
  

$$
\frac{dS}{dt} \ge -(\beta I + \mu + \xi)S
$$

integrating

$$
\int \frac{dS}{S} \ge -\int (\beta I + \mu + \xi) dt
$$

to obtain

$$
\ln S \ge -[\beta \int I(t) + \mu(t) + \xi(t)] + \ln c_1 \quad \text{at } t = 0 \text{ and } \ln c_1 = \ln S_0
$$

so that we have

$$
\ln\left(\frac{S(t)}{S_0}\right) \ge -\mu t - \xi t - \beta \int I(t)dt
$$

Taking exponentials of both sides

$$
S(t) \ge S_0 e^{-(\mu + \xi)t - \beta \int I(t)dt}
$$

Therefore the first equation of the system (3.1) is positive for all  $t >$ , since  $e^t > 0$  for all  $t \in \mathbb{R}$ 

For the second equation

$$
\frac{dD}{dt} = \xi S - \mu D - (1 - \delta)\beta DI
$$

This implies

$$
\frac{dD}{dt} \ge -\mu - (1 - \delta)\beta D I \ge -(\mu + (1 - \delta)\beta I)D
$$

separating variables and integrating

$$
\int \frac{dD}{D} \ge -\int (\mu + (1 - \delta)\beta I)dt
$$

we obtain

$$
\ln D(t) \ge -\mu t - \int (1 - \delta)\beta I(t)dt + \ln c_2 \quad \text{at } t = 0, \text{ and } \ln c_2 = \ln D_0
$$

gives

$$
\ln\left(\frac{D(t)}{D_0}\right) \ge -\mu t - \int (1-\delta)\beta I(t)dt
$$

Taking exponentials on both sides

$$
\frac{D(t)}{D_0} \ge e^{-\mu t - \int (1-\delta)\beta I(t)dt}
$$

which equivalently be written as

$$
D(t) \ge D_0 e^{-\mu t - \int (1 - \delta)\beta I(t)dt}
$$

Therefore the second equation of the system (3.1) is also positive for all  $t > 0$  since  $e^t > 0$  for all  $t \in \mathbb{R}$ 

In the third equation of the system (3.1)

$$
\frac{dI}{dt} = \beta SI + (1 - \delta)\beta DI - (\mu + \kappa + \sigma)I
$$

implying

$$
\frac{dI}{dt} \ge -(\mu + \kappa + \alpha)I
$$

separating the variables and integrating

$$
\int \frac{dI}{I} \ge -\int (\mu + \kappa + \sigma) dt
$$

yields

$$
\ln I(t) \ge -(\mu + \kappa + \sigma)t + \ln c_3 \quad \text{at} \quad t = 0 \quad \text{and} \quad \ln c_3 = \ln I_0
$$

$$
\ln\left(\frac{I(t)}{I_0}\right) \ge -(\mu + \kappa + \sigma)t
$$

taking exponentials on both sides,

$$
I(t) \ge I_0 e^{-(\mu + \kappa + \sigma)t}
$$

therefore the third equation of the system (3.1) is also positive for all  $t > 0$ , since  $e^t > 0$  for all  $t \in \mathbb{R}$ 

From the fourth equation of the system (3.1)

$$
\frac{dR}{dt} = \kappa I - \mu R \quad \text{implying} \quad \frac{dR}{dt} \ge -\mu R
$$

separating the variables and integrating

$$
\int \frac{dR}{R} \ge -\int \mu dt
$$

giving

$$
\ln R(t) \ge -\mu t + \ln c_4 \qquad t = 0 \quad and \quad \ln c_4 = \ln R_0
$$

$$
\ln \left( \frac{R(t)}{R_0} \right) \ge -\mu t
$$

taking exponentials on both sides

$$
R(t) \ge R_0 e^{-\mu t} \qquad R(t) \ge 0 \quad \forall t > 0
$$

This implies that all the state variables are non negative for all  $t > 0$ 

#### **3.2 Boundedness of solutions**

By showing that the solutions are bounded implies that the model is epidemiologically well posed in  $\Omega$  where  $\Omega = (S, D, I, R)$  By adding the 4 equations in the system (3.1) to obtain the total population size as

$$
N(t) = S(t) + D(t) + I(t) + R(t)
$$
\n(3.2)

This gives

<span id="page-5-0"></span>
$$
\frac{dN}{dt} = \frac{dS}{dt} + \frac{dD}{dt} + \frac{dI}{dt} + \frac{dR}{dt}
$$
  
=  $\pi - \mu S - \mu D - \mu I - \mu R - \sigma I$   
=  $\pi - (S + D + I + R)\mu - \sigma I$ 

and from (3.2)

$$
\frac{dN}{dt} = \pi - \mu N - \sigma I \tag{3.3}
$$

*Proof.* Let  $\Omega = (S, D, I, R) \in \mathbb{R}^4_+$  be any solution of the model equation with non-zero condition. In the absence of infection or disease, equation (3.3) becomes

$$
\frac{dN}{dt} \le \pi - \mu N
$$

that can be rearranged to give

$$
\frac{dN}{dt} + \mu N \le \pi \tag{3.4}
$$

This is a linear first order differential equation that can be solved by multiplying both sides of equation (3.4) by the integrating factor  $e^{\mu t}$ , gives

$$
e^{\mu} \frac{dN}{dt} + \mu Ne^{\mu t} \le \pi e^{\mu t}
$$

$$
d[Ne^{\mu t}] \le \pi e^{\mu t} dt
$$

integrating both sides, we have

$$
Ne^{\mu t} \leq \frac{\pi}{\mu}e^{\mu t} + c
$$
  

$$
N(t) \leq \frac{\pi}{\mu} + ce^{-\mu t}
$$

Applying the initial conditions at

$$
t = 0,
$$
  $N(0) = N_0 \leq \frac{\pi}{\mu} + c$   $\Rightarrow$   $N_0 - \frac{\pi}{\mu} \leq c$ 

and we now have

<span id="page-6-0"></span>
$$
N(t) \leq \frac{\pi}{\mu} + \left[ N_0 - \frac{\pi}{\mu} \right] e^{-\mu t}
$$
\n(3.5)

as  $t \to \infty$  in equation (3.5), the human population *N* approaches  $K = \frac{\pi}{\mu}$  i.e  $N \to K$ . The parameter  $K = \frac{\pi}{\mu}$  is the carrying capacity. Hence *N* is bounded and all feasible solution sets of the population of the model system approach or stay in the region

$$
\Omega = \left\{ S, D, I, R \in \mathbb{R}_+^4 : S \ge 0, \ D \ge 0, \ I \ge 0, \ R \ge 0, \ N \le \frac{\pi}{\mu} \right\}
$$

The region  $\Omega$  is therefore positively invariant, that is the solution is positive for all time t and the model system is epidemiologically meaningful and Mathematical well posed in the domain  $\Omega$ . Hence it is sufficient to consider the dynamics of the flow it generates in a proper subset

$$
\Omega = \{ (S, D, I, R) \in \mathbb{R}_+^4 \}
$$

# **4 Equilibria Points of the Model**

Analysing the model to investigate the stability of its equilibria both at disease-free equilibrium (DFE)and disease -endemic equilibria (DEE). The disease-free equilibrium points of the model are its steady states solutions in the absence of infection, [20]. Equilibria points of the model system in equation (3.1)is obtained by equating the derivatives to zero and solve for the variables

$$
\pi - \beta SI - \mu S - \xi S = 0
$$
  
\n
$$
\xi S - \mu D - (1 - \delta)\beta DI = 0
$$
  
\n
$$
\beta SI + (1 - \delta)\beta DI - (\mu + \kappa + \sigma)I = 0
$$
  
\n
$$
\kappa I - \mu R = 0
$$
\n(4.1)

Using  $S + E = \frac{\pi}{\mu}$  it can be shown that at disease free equilibrium of the model system equation (3.1)

$$
\pi - \mu S - \xi S = 0 \Rightarrow S = \frac{\pi}{\mu + \xi}
$$
  

$$
\xi S - \mu D = 0 \Rightarrow D = \frac{\xi S}{\mu}
$$
  

$$
D = \frac{\xi \pi}{\mu(\mu + \xi)}
$$

$$
DFE = (S^{0}D^{0}I^{0}R^{0})
$$
  
= 
$$
(\frac{\pi}{\mu+\xi}, \frac{\xi\pi}{\mu(\mu+\xi)}, 0, 0)
$$

# **5 Basic Reproduction Number**

**Definition 5.1** (Basic Reproduction Number, [11]). The basic reproduction number  $R_0$  in a given population is the average number of secondary infection caused by a single infectious individual during his/her entire lifetime as an infection when introduced into a totally or purely susceptible population.

The dynamics of the model are highly depen[den](#page-17-10)t on the basic reproduction number  $R_0$  in that *π* is directly related to the effort required to eliminate the infection. In this paper, the basic reproduction number *R<sup>D</sup>* is the expected number of secondary SARS-nCoV 2 infection caused by a single infected individual in the presence of social distance awareness intervention, when no such kind of programmes are employed. We determine *R<sup>D</sup>* using the next generation matrix approach, [11].

Consider a matrix

$$
G = FV^1
$$

[whe](#page-17-10)re *F* is the Jacobian of  $f_j$ , where  $f_j$  is the rate of new infections in compartment *j* and *V* is the Jacobian of  $V_j$ , where  $V_j$  is the rate of transfer of infections from one compartment to another. From the system model equation (3.1)

$$
\mathcal{F} = \begin{pmatrix} \beta SI + (1 - \delta)\beta DI \\ 0 \end{pmatrix}
$$

$$
\mathcal{V} = \begin{pmatrix} (\sigma + \mu + \kappa +)I \\ (0 \\ 0 \end{pmatrix}
$$

$$
F = \begin{pmatrix} \beta S + (1 - \delta)\beta D & 0 \\ 0 & 0 \end{pmatrix}
$$

at disease-free equilibrium DFE,

$$
S = \frac{\pi}{\xi + \mu} \quad \text{and} \quad D = \frac{\xi \pi}{\mu(\mu + \xi)}
$$

$$
F = \begin{pmatrix} \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} & 0 \\ 0 & 0 \end{pmatrix}
$$

$$
V = \begin{pmatrix} \sigma + \mu + \kappa \\ 0 \\ 0 \end{pmatrix}
$$

we consequently determine

$$
V^{-1} = \left(\begin{array}{c} \frac{1}{\sigma + \mu + \kappa} \\ 0 \end{array}\right)
$$

therefore

$$
FV^{-1} = \begin{pmatrix} \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} \frac{1}{\sigma + \mu + \kappa} \\ 0 \end{pmatrix}
$$

$$
FV^{-1} = \begin{pmatrix} \frac{1}{\sigma + \mu + \kappa} \left( \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} \right) & 0 \\ 0 & 0 \end{pmatrix}
$$

computing the eigenvalues from the characteristic equation

$$
\begin{bmatrix}\n\left(\frac{1}{(\mu+\kappa+\alpha)}\left[\frac{\beta\pi}{\mu+\xi}+(1-\delta)\frac{\beta\xi\pi}{\mu(\xi+\mu)}\right]-\lambda\right) & 0 \\
0 & -\lambda\n\end{bmatrix} = 0
$$

and obtain

$$
\lambda_1 = 0,
$$
\n $\lambda_2 = \frac{1}{(\mu + \kappa + \alpha)} \left[ \frac{\beta \pi}{(\mu + \xi)} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} \right]$ 

for

$$
\lambda_2 = \frac{\beta \mu \pi + (1 - \delta)\beta \xi \pi}{\mu(\mu + \xi)(\mu + \kappa + \alpha)}
$$

$$
= \frac{\beta \pi}{\mu(\mu + \kappa + \alpha)} \left(\frac{\mu + (1 - \delta)\xi}{(\xi + \mu)}\right) = R_D
$$

Therefore

$$
R_D = \frac{\beta \pi}{\mu(\mu + \kappa + \alpha)} \left( \frac{\mu + (1 - \delta)\xi}{(\xi + \mu)} \right)
$$

In the absence of social distancing intervention ,  $\xi = 0$  and the basic reproduction number becomes

$$
R_0 = \frac{\beta \pi}{\mu(\mu + \kappa + \alpha)} \left( \frac{\mu + (1 - \delta)0}{(0 + \mu)} \right)
$$

$$
= \frac{\beta \pi}{\mu(\mu + \kappa + \alpha)}
$$

This implies

$$
R_D = R_0 \left[ \frac{\mu + (1 - \delta)\xi}{\mu + \xi} \right]
$$
\n(5.1)

Since we have the set  $0 < \xi < 1$ , it follows that

$$
\left(\frac{\mu+(1-\delta)\xi}{\mu+\xi}\right) < 1
$$

which implies  $R_D < R_0$ .It is clear that social distancing intervention on transmission of SARSnCoV2 has a positive impact on the reduction of new infections.It is important to note that we have used the next generation matrix approach in estimating the basic reproduction number; however there exist other methods, including obtaining the eigenvalues of the Jacobian matrix, the survival function technique and existence of endemic equilibrium which can be employed in models where computations are not successful, [21].

### **6 Stability Analysis**

#### **6.1 Local stability an[d d](#page-18-5)isease free equilibrium**

Further analysis of the model to investigate the stability of its equilibrium. The disease-free equilibrium point of the model is its steady states solution in the absence of disease or infection.

**Theorem 6.1.** *The disease-free equilibrium of the model system* (3.1) *is locally asymptotically stable whenever*  $R_D < 1$  *and unstable whenever*  $R_D > 1$ 

*Proof.* We prove the theorem by obtaining the eigenvalues of the Jacobian matrix of the linearised system given by

$$
J = \begin{pmatrix} -\beta I - \mu - \xi & 0 & -\beta S & 0 \\ 0 & -(\mu + (1 - \delta)\beta I & -(1 - \delta)\beta D & 0 \\ \beta I & (1 - \delta)\beta I & \beta S + (1 - \delta)\beta D & 0 \\ 0 & 0 & \kappa & \mu \end{pmatrix}
$$

We now compute the Jacobian matrix at DFE and investigate its stability effect due to the reproduction number  $R_D$ . The Jacobian matrix at DFE  $S^0 D^0 I^0 R^0$  is given by

$$
J(D^{0}) \begin{pmatrix} -(\xi + \mu) & 0 & \frac{-\beta \pi}{\xi + \mu} & 0 \\ 0 & -\mu & -(1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} & 0 \\ 0 & 0 & \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} & 0 \\ 0 & 0 & \kappa & -\mu \end{pmatrix}
$$

The characteristic equation is given by

$$
|(J(D^0) - \lambda I)| = 0
$$

$$
|J(D^{0}) - \lambda I| = \begin{vmatrix} -(\xi + \mu + \lambda) & 0 & \frac{-\beta \pi}{\xi + \mu} & 0\\ 0 & -\mu - \lambda & -(1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} & 0\\ 0 & 0 & \left[ \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} - (\sigma + \kappa + \mu) \right] - \lambda & 0\\ 0 & 0 & \kappa & -(\mu + \lambda) \end{vmatrix}
$$

We obtain the following eigenvalues

$$
\lambda_1 = -(\xi + \mu)
$$
  
\n
$$
\lambda_2 = -\mu
$$
  
\n
$$
\lambda_3 = \frac{\beta \pi}{\xi + \mu} + (1 - \delta) \frac{\beta \xi \pi}{\mu(\mu + \xi)} - (\sigma + \kappa + \mu)
$$
  
\n
$$
\lambda_4 = -\mu
$$

From  $\lambda_3$ , we have

$$
\lambda_3 = \frac{\beta \mu \pi + (1 - \delta) \beta \xi \pi - \mu (\mu + \xi) (\mu + \kappa + \sigma)}{\mu (\mu + \xi)}
$$

But

$$
R_D = \frac{\beta \mu \pi + (1 - \delta)\beta \xi \pi}{\mu(\mu + \xi)(\mu + \kappa + \sigma)}
$$

This implies

$$
\lambda_3 = (R_D - 1)(\mu + \kappa + \sigma)
$$

If  $R_E$  < 1 then  $\lambda_3$  is also negative. This clearly shows that  $\lambda_1, \lambda_2, \lambda_3, \lambda_4$  are all negative. The eigenvalues have negative real parts from Routh-Hurwitz criterion [22, 23]. Therefore the diseasefree equilibrium is locally asymptotically stable in the region  $\Omega$  if and only if  $R_D < 1$ , and unstable if  $R_D > 1$ . Hence the theorem is proved.  $\Box$ 

#### **6.2 Global Stability of the disease-free equili[br](#page-18-6)i[um](#page-18-7)**

The global stability of the disease-free equilibrium (DFE)is easily proved using a common Lyapunov function and La Salles' invariance principal.

**Theorem 6.2.** If  $R_D \leq 0$  then the disease-free equilibrium of the model system (3.1) is globally *asymptotically stable in the region* Ω*.*

*Proof.* To prove the theorem, we begin by constructing a linear Lyapunov function We define

$$
L: \{(S, D, I, R) \in \Omega : , S, D > 0\} \to \mathbb{R}
$$

by

$$
L(S, D, I, R) = (\mu + \kappa + \alpha)I
$$

The global stability of disease free equilibrium holds if its time derivative  $\frac{dL}{dt} \leq 0$  The time derivative of Lyapunov function *L* is given by

$$
\frac{dL}{dt} = (\mu + \kappa + \sigma)I'
$$
\n
$$
= (\mu + \kappa + \sigma)(\beta SI + (1 - \delta)\beta DI) - (\mu + \kappa + \sigma)
$$
\n
$$
\leq (\mu + \kappa + \sigma) \left[\beta(S + D) - (\mu + \kappa + \sigma)\right]I \quad \text{but} \quad S + D = \frac{\pi}{\mu}
$$
\n
$$
\leq (\mu + \kappa + \sigma) \left(\frac{\beta \pi}{\mu} - (\mu + \kappa + \sigma)\right)
$$
\n
$$
\leq (R_0 - 1)(\mu + \kappa + \sigma)(\mu + \kappa + \sigma)I
$$

Since  $R_D < R_0$  in  $o < \xi < 1$  We have

$$
\frac{dL}{dt} \le (R_D - 1)(\mu + \kappa + \sigma)^2 I
$$

If  $\frac{dL}{dt} = 0$ , then  $I = 0$ . hence *L* is a Lyapunov function on  $\Omega$ . Thus  $I \to 0$  as  $t \to \infty$  substituting *I* = 0 in equation (3.1) we obtain  $S + D = \frac{\pi}{\mu}$ . It therefore follows from La Salles invariance principle that every solution of the model system equation (3.1) with the initial condition in  $\Omega$ , approaches DFE as  $t \to \infty$ □

#### **6.3** Existen[ce](#page-3-0) of a unique positive endemic equilibrium  $E^*(S^*D^*I^*R^*)$

**Lemma 6.3.** An endemic equilibrium  $E^*(S^*D^*I^*R^*)$  $E^*(S^*D^*I^*R^*)$  $E^*(S^*D^*I^*R^*)$  exists provided that  $R_D > 1$ 

*Proof.* At endemic state, equation (3.1) becomes

$$
\pi - \beta S_* I_* - \mu S_* - \xi S_* = 0 \tag{6.1}
$$

$$
\xi S_* - \mu D_* - (1 - \delta) \beta D_* I_* = 0 \tag{6.2}
$$

<span id="page-11-5"></span>
$$
\beta S_* I_* + (1 - \delta) \beta D_* I_* - (\sigma + \mu + \kappa) I_* = 0 \tag{6.3}
$$

<span id="page-11-0"></span>
$$
\kappa I_* - \mu R_* = 0 \tag{6.4}
$$

To calculate the disease endemic equilibrium DEE, we set  $(S, D, I, R) \neq 0$  and solving for  $S^*$  in (6.1)

<span id="page-11-1"></span>
$$
S_* = \frac{\pi}{\beta I_* + \mu + \xi} \tag{6.5}
$$

solving for  $E_*$  from equation (6.2)

<span id="page-11-2"></span>
$$
D_* = \frac{\xi S_*}{\mu + (1 - \delta)\beta I_*} \tag{6.6}
$$

From equation (6.3)

$$
(\beta S_* + (1 - \delta)\beta D_* - (\sigma + \mu + \kappa)I_* = 0
$$

but at Disease Endemic Equilibrium  $I_* \neq 0$ 

$$
\beta S_* + (1 - \delta)\beta D_* - (\sigma + \mu + \kappa) = 0
$$

$$
S_* = \frac{(\sigma + \mu + \kappa) - (1 - \delta)\beta D_*}{\beta} \tag{6.7}
$$

and from equation (6.4)

<span id="page-11-3"></span>
$$
R_* = \frac{\kappa I_*}{\mu} \tag{6.8}
$$

To obtain the value of  $I_*$  we equate equations (6.5) and (6.7) with correct substitution for  $D_*$ , so that we have

$$
\frac{\sigma + \mu + \kappa}{\beta} \left[ \frac{\mu + (1 - \delta)\beta I_*}{\mu + (1 - \delta)\beta I_* + (1 - \delta)\xi} \right] = \frac{\pi}{\beta I_* + \xi + \mu} \tag{6.9}
$$

solving for *I<sup>∗</sup>* from the above equation, we have

$$
(1 - \delta)\beta^2(\sigma + \mu + \kappa)I_*^2 + [\beta\mu(\sigma + \mu + \kappa) + (1 - \delta)\beta(\mu\sigma + \mu^2 + \xi\kappa - \beta\pi)]
$$
  

$$
[\mu + (\sigma + \mu + \kappa) - \beta\pi(1 + (1 - \delta)\xi)] = 0
$$
 (6.10)

<span id="page-11-4"></span>Equation (6.10) can be expressed quadratically as

$$
AI_*^2 + BI_* + C = 0
$$

where

$$
A = (1 - \delta)\beta^2(\sigma\mu + \kappa)
$$
  
\n
$$
B = \beta\mu(\sigma + \mu + \kappa) + (1 - \delta)\beta(\mu\sigma + \mu^2\xi\kappa - \beta\pi)
$$
  
\n
$$
C = \mu(\mu + \sigma\kappa) - (\beta\pi + \beta\pi\xi(1 - \delta))
$$

since

I I I I I I I I I I I I I ļ

$$
R_D = \frac{\beta \pi}{\mu + (\mu + \kappa + \sigma)} \left[ \frac{\mu + (1 - \delta)\xi}{\mu + \xi} \right] > 1
$$

It is easy to show that

$$
\beta \pi + \beta \pi \xi (1 - \delta) > \mu (\mu + \sigma + \kappa)
$$

This clearly proves that  $C < 0$  when  $R_D > 1$ . Equation (6.10) can only be expressed as either

$$
AI_*^2 + BI_* - C = 0
$$

and by Descartes rule,[24]. There is only one positive root of equation (6.10), that is  $I^* > 0$ . We therefore conclude that there exist one unique positi[ve d](#page-11-4)isease endemic equilibrium whenever  $R_D > 0$  $\Box$ 

#### **6.4 Local stabi[lit](#page-18-8)y of the endemic equilibrium**

**Theorem 6.4.** *If*  $R_D > 1$ , *then the disease-endemic equilibrium of the model system* (3.1) *is locally asymptotically stable*

*Proof.* A disease is endemic in a population if it persist in the population. We investigate the stability of the  $E_*(S_*D_*I_*R_*)$  using the Routh-Hurwitz criterion

The Jacobian matrix at  $E_*(S_*D_*I_*R_*)$  given by

$$
J_{D^*} = \begin{pmatrix} -\beta I_* - (\mu + \xi) & 0 & -\beta S_* & 0 \\ \xi & -(\mu + (1 - \delta)\beta I_*) & - (1 - \delta)\beta D_* & 0 \\ \beta I_* & (1 - \delta)\beta I_* & [(\mu + \kappa + \sigma - \beta S_* - (1 - \delta)\beta D_*] & 0 \\ 0 & 0 & \kappa & -\mu \end{pmatrix}
$$

The characteristic equation is given by

$$
|J(E^*) - \lambda I| = 0
$$

$$
-(\beta I_{*} + \mu + \xi) - \lambda \qquad 0 \qquad -\beta S_{*} \qquad 0
$$
  

$$
\xi \qquad -(\mu + (1 - \delta)\beta I_{*}) - \lambda \qquad -(1 - \delta)\beta D_{*} \qquad 0
$$
  

$$
\beta I_{*} \qquad (1 - \delta)\beta I_{*} \qquad (\mu + \kappa + \sigma) - \beta S_{*} - (1 - \delta)\beta D_{*} - \lambda \qquad 0
$$
  

$$
0 \qquad 0 \qquad \kappa \qquad -\mu - \lambda
$$

The characteristic equation associated with the Jacobian matrix above is given by

$$
B_0 \lambda^4 + B_1 \lambda^3 + B_2 \lambda^2 + B_3 \lambda + B_4 = 0 \tag{6.11}
$$

where

$$
B_0 = 1
$$
  
\n
$$
B_1 = \mu + d_1 + d_3 + d_5
$$
  
\n
$$
B_2 = d_1(d_2 + d_5 + \mu) + d_2(d_5 + \mu) + d_3d_4
$$
  
\n
$$
B_3 = d_1d_2(\mu + d_5) + \mu d_5(d_1 + d_2) + d_3d_4(d_1 + \mu)
$$
  
\n
$$
B_4 = d_1\mu(d_2d_5 + d_3d_4) + d_4\xi\mu\beta S_*
$$

and

$$
d_1 = \beta I_* + \mu + \xi
$$
  
\n
$$
d_2 = \mu + (1 - \delta)\beta I_*
$$
  
\n
$$
d_3 = (1 - \delta)\beta D_*
$$
  
\n
$$
d_4 = (1 - \delta)\beta I_*
$$
  
\n
$$
d_5 = (\mu + \kappa + \alpha) - \beta S_* - (1 - \delta)\beta D_*
$$

From equation (6.11), the constants  $B_0$ ,  $B_1$ ,  $B_2$ ,  $B_3$ , and  $B_4$  are all positive. Now using Routh-Hurwitz criterion for a fourth degree polynomial [22], to ascertain the stability of the characteristic equation which satisfy the necessary condition for Routh-Hurwitz criterion, we next verify the sufficient condition for the Routh- Hurwitz criterion of stability. Therefore constructing the Routh array;

$$
\begin{array}{c|cc}\n\lambda^4 & B_0 & B_2 & B_4 \\
\lambda^3 & B_1 & B_3 & 0 \\
\lambda^2 & a_1 & B_4 & 0 \\
\lambda^1 & a_2 & 0 & 0 \\
\lambda^0 & B_4 & 0 & 0\n\end{array}
$$

where

$$
a_1 = \frac{B_1 B_2 - B_0 B_3}{B_1} > 0 \quad \text{for} \quad B_1 B_2 > B_0 B_3
$$
\n
$$
a_2 = B_3 - \frac{B_1^2 B_4}{B_1 B_2 - B_0 B_3} > 0 \quad \text{for} \quad B_3 > \frac{B_1^2 B_4}{B_1 B_2 - B_0 B_3}
$$

All the elements of the first column of the Routh array are positive. There is no sign change in the first column of the Routh array which is the sufficient condition for the Routh-Hurwitz stability. Hence the endemic equilibrium is locally asymptotically stable.  $\Box$ 

#### **6.5 Global stability of the endemic equilibrium of the model (EE)**

To prove the global stability of the endemic equilibrium, $E^*$  under the condition  $R_D > 1$  we apply the Lyapunov function [22, 23, 25], that takes advantage of the property of the function.

$$
h(x) = x - 1 - \ln(x)
$$

which is positive in  $(0, \infty)$  except at  $x = 1$  where it vanishes

**Theorem 6.5.** *The endemic equilibrium E ∗ of the model* (3.1) *is globally asymptotically stable in*  $Ω$  *whenever*  $R_D > 1$ 

*Proof.* Consider the following Logarithmic Lyapunov function *V* defined by

$$
V(S, E, I, R) = \sum_{i=1}^{4} (x_i - x_i^* \ln x_i)
$$

*x*<sub>i</sub> is the population of the *i*<sup>th</sup> compartment while  $x_i^*$  is the equilibrium value of  $x_i$ . Lyapunov function denoted by *V* is continuous and differentiable. The global stability of the endemic equilibrium holds if its time derivative  $\frac{dV}{dt} \leq 0$ . The time derivative of Lyapunov function *V* is given by

$$
\frac{dV}{dt}(S, E, I, R) = \sum_{i=1}^{4} \left(1 - \frac{x_i^*}{x_i}\right) \frac{dx_i}{dt}
$$

so that we have

$$
\frac{dV}{dt} = \left(1 - \frac{S^*}{S}\right)\frac{dS}{dt} + \left(1 - \frac{D^*}{D}\right)\frac{dD}{dt} + \left(1 - \frac{I^*}{I}\right)\frac{dI}{dt} + \left(1 - \frac{R^*}{R}\right)\frac{RS}{dt}
$$
\n
$$
= \left(1 - \frac{S^*}{S}\right)\left[\pi - \beta SI - \mu S - \xi S\right] + \left(1 - \frac{D^*}{D}\right)\left[\xi S - \mu D - (1 - \delta)\beta DI\right]
$$
\n
$$
+ \left(1 - \frac{I^*}{I}\right)\left[\beta SI + (1 - \delta)\beta DI - (\mu + \kappa + \sigma)I\right] + \left(1 - \frac{R^*}{R}\right)\left[\kappa I - \mu R\right] \quad (6.12)
$$

<span id="page-14-3"></span>An endemic equilibrium  $S' = D' = I' = R' = 0$ , we therefore can have the following substitutions From equation (6.1), we have

$$
\pi = \beta S^* I^* + \mu S + \xi S^* \tag{6.13}
$$

From equation (6.2), we have

$$
(\mu + \kappa + \sigma) = \left(\frac{\beta S^* I^* + (1 - \delta)\beta D^* I^*}{I^*}\right)
$$
\n(6.14)

From equation ([6.3](#page-11-0)), we have

<span id="page-14-0"></span>
$$
\beta = \left(\frac{\xi S^* + \mu D^*}{(1 - \delta) D^* I^*}\right) \tag{6.15}
$$

from equation ([6.4\)](#page-11-5). Next we make

<span id="page-14-2"></span><span id="page-14-1"></span>
$$
\kappa = \frac{\mu R^*}{I^*} \tag{6.16}
$$

Using equations  $(6.13),(6.14),(6.15)$  and  $(6.16)$  to rewrite equation  $(6.12)$  and simplifications yields

$$
\frac{dV}{dt} = (\mu + \xi)S^*\left(2 - \frac{S^*}{S} - \frac{S}{S^*}\right) + \left(1 - \frac{S^*}{S}\right)\left(1 - \frac{SI}{S^*I^*}\right)
$$

$$
+ \left(1 - \frac{D^*}{D}\right) + \left[\xi\left(1 - \frac{S^*DI}{SD^*I^*}\right) - \mu\left(1 + \frac{I}{I^*}\right)\right]
$$

$$
+ \left(1 - \frac{I^*}{I}\right)\left(\frac{\xi S^* + \mu D^*}{D^*}\right)\frac{I}{I^*}\left[\frac{1}{1 - \delta}\left(1 - \frac{S^*}{S}\right) + \left(1 - \frac{D^*}{D}\right)\right]
$$

$$
+ \left(1 - \frac{R^*}{R}\right)\left[1 - \frac{I^*R}{IR^*}\right]
$$



At

$$
S = S^*, \quad D = D^*, \quad I = I^* \quad R = R^*
$$

and from the property that the geometric mean and is less than or equal to arithmetic mean, the inequality  $\frac{dV}{dt} \leq 0$  holds if and only if (S,D,I,R) takes the equilibrium values  $S^*D^*I^*R^*$ . Therefore, by La Salle's invariance Principle,[26] the endemic equilibrium *E ∗* is globally asymptotically stable. Global asymptotic stability shows that regardless of any solution,the solution of the model will converge at *E <sup>∗</sup>* whenever *R<sup>D</sup> >* 1. Epidemiologically, any perturbation of the model solution by the introduction of infectives shows that the model solution will converge to the  $E^*$  whenever  $R_D > 1$ 

### **7 Numerical Simulations**

Numerical simulations were carried using MATLAB R2021b to one, understand the complex asymptomatic infectious individuals with regards to reproduction number and secondly to graphically illustrate the long term effect of social distance intervention on the dynamics 2019-nCov/SARS-CoV2 infection. The solution of the model above is done using parameter values shown in table below:

**Table 2. Detailed description of the state variables and relevant parameters of the proposed SDIR Covid 19 Model**

Detailed Description	Symbol	Value	Source
Susceptible Population	S(t)	$5.4 \times 10^7$	$\left[ 27\right]$
Susceptible Recruitment Rate	$\pi$	0.1545	[7]
Natural Death Rate	$\mu$	$5.2 \times 10^{-8}$	$\left[ 27\right]$
Death Rate due to Covid 19	$\sigma$	$2.607 \times 10^{-7}$	$\lceil 7 \rceil$
Recovered Reverting Rate to Susceptible	$\kappa$	$6.75 \times 10^{-1}$	Assumed
Effective Contact Transmission Rate	В	$2.985 \times 10^{-8}$	Computed
Social Distance Intervention Rate	$\theta$	0.75	Assumed
Social Distance Awareness Rate		$1.75 \times 10^{-7}$	Computed



**Fig. 2. Spread of SARS-nCov2 Keeping Social Distance**



**Fig. 3. Spread of SARS-nCov2 Without Keeping Social Distance**

### **8 Discussion**

Based on illustrations from Fig. 2, it is clear that the population of the susceptible individuals shortly starts dropping due to social distancing intervention, consequently the recovered individuals starts to rise. The number of 2019-nCoV/SARS-nCoV2 infected individuals increase for a short period then decreases before stabilising below the susceptible population. This is an indication that social distancing intervention is key to reduction in the infection rate of 2019-nCoV/SARS-nCoV2 hence public gatherings in political rallies, worship centers,market places, football matches should be put on hold. The ministry of health and in particular, department of public health together with other stakeholders should suggest measures where social distancing is kept. Similarly Fig. 3 with a slight decrease in social distancing intervention  $\delta$  i.e the population of exposed population becomes apparently high and the recovered population also reduces.

# **9 Conclusion and Recommendations**

In this study, a deterministic mathematical model based on systems of ordinary differential equations for the dynamics of 2019-nCoV/SARS-CoV2 transmission incorporating social distancing as a control measure was derived. The stability of the disease free and endemic equilibrium have been analysed. The results of the disease free equilibrium showed that the model is both locally and globally stable when  $R_{SE}$   $\lt$  1 thus reducing  $R_{SE}$  to less than unity reduces the spread of the disease. Endemic equilibrium has also been analysed and was found to be locally asymptotically stable when  $R_{SE}$  < 1. From the numerical simulation, it is clear that the public health sector should consider keeping social distancing during public gatherings in political rallies, worship centers,market places, football matches as a major intervention strategy for low 2019-nCoV/SARS-nCoV2 infection rate.

### **Competing Interests**

Author has declared that no competing interests exist.

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<span id="page-18-9"></span> $\mathcal{L}=\{1,2,3,4\}$  , we can consider the constant of the constant  $\mathcal{L}=\{1,2,3,4\}$ *⃝*c *2022 Achola; This is an Open Access article distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/4.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.*

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